

International
Scientific Conference



Algebraic
and Geometric
Methods
of Analysis

27-30 May 2024
Odesa, Ukraine

The purpose of this conference is to bring together researchers in geometry, topology, algebra, analysis and dynamical systems and to provide for them a forum to present their recent work to colleagues from different nationalities. This way we aim to stimulate discussion about the latest findings in geometrical and topological methods in analysis and to increase international collaboration.

The conference continues the traditional annual conference «Geometry in Odesa» holding from 2004, and hosted by Odesa National University of Technology (Odesa National Academy of Food Technologies till 2021). From 2017 the conference was renamed to «Algebraic and geometric methods of analysis» (AGMA).

The Conference languages: Ukrainian and English.

LIST OF TOPICS

- Algebraic methods in geometry
- Differential geometry in the large
- Geometry and topology of differentiable manifolds
- General and algebraic topology
- Dynamical systems and their applications
- Geometric and topological methods in natural sciences
- Geometric problems in mathematical analysis

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On some nonlocal critical equations

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Aim of this talk will be to discuss some existence and multiplicity results for critical nonlocal fractional problems got via variational and topological methods. In particular we will present recent contributions got in the joint paper [1].

Fractional and nonlocal operators appear in various models coming from many different fields. This is one of the reason why, recently, nonlocal fractional problems attracted the interest of the entire scientific community and not just the mathematical one.

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On boundary estimates of mappings, acting onto domains with a locally quasiconformal boundary

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The following definitions are from [1]. A path γ in \mathbb{R}^n is a continuous mapping $\gamma : \Delta \rightarrow \mathbb{R}^n$ where Δ is an interval in \mathbb{R} . Its locus $\gamma(\Delta)$ is denoted by $|\gamma|$. Given a family Γ of paths γ in \mathbb{R}^n , a Borel function $\rho : \mathbb{R}^n \rightarrow [0, \infty]$ is called *admissible* for Γ , abbr. $\rho \in \text{adm } \Gamma$, if $\int_{\gamma} \rho(x) |dx| \geq 1$ for each (locally rectifiable) $\gamma \in \Gamma$. The *modulus* of Γ is defined by the relation

$$M(\Gamma) := \inf_{\rho \in \text{adm } \Gamma} \int_{\mathbb{R}^n} \rho^n(x) dm(x) \quad (1)$$

interpreted as $+\infty$ if $\text{adm } \Gamma = \emptyset$. Everywhere below, unless otherwise stated, the boundary and the closure of a set are understood in the sense of the extended Euclidean space $\overline{\mathbb{R}^n}$.

Let $Q : \mathbb{R}^n \rightarrow [0, \infty]$ be Lebesgue measurable function. We will say that f satisfies the inverse Poletsky's inequality if the ratio

$$M(\Gamma) \leq \int_{f(D)} Q(y) \cdot \rho_*^n(y) \, dm(y) \tag{2}$$

holds for any family of (locally rectifiable) paths Γ in D and for any $\rho_* \in \text{adm } f(\Gamma)$. Note that estimates of the type (2) are well known and holds for classes of mappings (see, e.g., [2, Theorem 6.7.II] and [3, theorem 8.5]).

Given sets E and F and a given domain D in $\overline{\mathbb{R}^n} = \mathbb{R}^n \cup \{\infty\}$, we denote by $\Gamma(E, F, D)$ the family of all paths $\gamma : [0, 1] \rightarrow \overline{\mathbb{R}^n}$ joining E and F in D , that is, $\gamma(0) \in E$, $\gamma(1) \in F$ and $\gamma(t) \in D$ for all $t \in (0, 1)$. In accordance with [4], a domain D in \mathbb{R}^n is called *quasiextremal distance domain* (*QED-domain for short*) if

$$M(\Gamma(E, F, \mathbb{R}^n)) \leq A_0 \cdot M(\Gamma(E, F, D)) \tag{3}$$

for some finite number $A_0 \geq 1$ and all continua E and F in D . In the extended Euclidean space $\overline{\mathbb{R}^n} = \mathbb{R}^n \cup \{\infty\}$ we use the *spherical (chordal) metric* $h(x, y) = |\pi(x) - \pi(y)|$, where π is a stereographic projection of $\overline{\mathbb{R}^n}$ onto the sphere $S^n(\frac{1}{2}e_{n+1}, \frac{1}{2}) = \{x \in \mathbb{R}^{n+1} : |x - e_{n+1}/2| = 1/2\}$ in \mathbb{R}^{n+1} , and

$$h(x, \infty) = \frac{1}{\sqrt{1 + |x|^2}},$$

$$h(x, y) = \frac{|x - y|}{\sqrt{1 + |x|^2} \sqrt{1 + |y|^2}}, \quad x \neq \infty \neq y \tag{4}$$

(see e.g. [1, Definition 12.1]). In what follows, given $A, B \subset \overline{\mathbb{R}^n}$ we set $h(A, B) = \inf_{x \in A, y \in B} h(x, y)$,

where h is a chordal metric in (4). Consider the following definition that has been proposed by Näkki [5], cf. [6]. The boundary of a domain D is called *locally quasiconformal* if every point $x_0 \in \partial D$ has a neighborhood U , for which there exists a quasiconformal mapping φ of U onto the unit ball $\mathbb{B}^n \subset \mathbb{R}^n$ such that $\varphi(\partial D \cap U)$ is the intersection of the unit sphere \mathbb{B}^n with a coordinate hyperplane $x_n = 0$, where $x = (x_1, \dots, x_n)$. Note that, with slight differences in the definition, domains with such boundaries are also called *collared domains*.

Given $\delta > 0$, domains $D, D' \subset \mathbb{R}^n$, $n \geq 2$, a nondegenerate continuum $A \subset D'$ and a Lebesgue-measurable function $Q : D' \rightarrow [0, \infty]$ denote by $\mathfrak{S}_{\delta, A, Q}(D, D')$ the family of all open discrete and closed mappings f of the domain D onto the domain D' satisfying the condition (2) and such that $h(f^{-1}(A), \partial D) \geq \delta$. The following statement is true.

Theorem 1. *Let $Q \in L^1(D')$, let D be a QED-domain, and D' is a bounded domain with a locally quasiconformal boundary. Then any mapping $f \in \mathfrak{S}_{\delta, A, Q}(D, D')$ which satisfies the relation (2) has a continuous extension $f : \overline{D} \rightarrow \overline{D}'$, while, for each point $x_0 \in \partial D$ there will be U neighborhoods of this point and constants $C = C(n, A, D, D', x_0) > 0$ and $0 < \alpha = \alpha(n, A, D, D', x_0) \leq 1$ such that*

$$|\overline{f}(x) - \overline{f}(y)|^{\frac{n}{\alpha^2}} \leq \frac{C \cdot \|Q\|_1}{\log \left(1 + \frac{\delta}{2|x-y|} \right)} \tag{5}$$

for all $x, y \in U \cap \overline{D}$, where $\|Q\|_1$ is the norm of the function Q in $L^1(D')$.

The result mentioned above is accepted for publication in [7].

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Some properties of affine ruled submanifolds

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We consider an affine ruled submanifolds of arbitrary dimension and codimension in the classical sense, that is, a ruled submanifolds over a curve.

Using the equiaffine theory of curves in an arbitrary affine space [1] we choose the most convenient parameterization and transversal distribution of the affine immersion of a ruled submanifold in general case, i. e., of arbitrary dimension and codimension.

All affine characteristics (induced connection, transversal connection, affine fundamental forms, Weingarten operators, curvature tensor) of such an affine immersion are found depending on the characteristics of the base curve and rectilinear generators.

We find the conditions for a base curve and directions of rectilinear generators so that the induced connection is flat. These conditions coincide with the already known properties of affine immersions with flat connection ([2]-[6]). Also we find the conditions for a base curve and directions of rectilinear generators so that the chosen transversal distribution is equiaffine.

Acknowledgment. The author acknowledge the partial support from the Akhiezer Foundation.

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