

International  
Scientific Conference



Algebraic  
and Geometric  
Methods  
of Analysis

27-30 May 2024  
Odesa, Ukraine

The purpose of this conference is to bring together researchers in geometry, topology, algebra, analysis and dynamical systems and to provide for them a forum to present their recent work to colleagues from different nationalities. This way we aim to stimulate discussion about the latest findings in geometrical and topological methods in analysis and to increase international collaboration.

The conference continues the traditional annual conference «Geometry in Odesa» holding from 2004, and hosted by Odesa National University of Technology (Odesa National Academy of Food Technologies till 2021). From 2017 the conference was renamed to «Algebraic and geometric methods of analysis» (AGMA).

The Conference languages: Ukrainian and English.

#### LIST OF TOPICS

- Algebraic methods in geometry
- Differential geometry in the large
- Geometry and topology of differentiable manifolds
- General and algebraic topology
- Dynamical systems and their applications
- Geometric and topological methods in natural sciences
- Geometric problems in mathematical analysis

#### ORGANIZERS

- Ministry of Education and Science of Ukraine
- Odesa National University of Technology, Ukraine
- Institute of Mathematics of the National Academy of Sciences of Ukraine
- Taras Shevchenko National University of Kyiv
- Kyiv Mathematical Society

#### SCIENTIFIC COMMITTEE

- |                                                       |                                                          |
|-------------------------------------------------------|----------------------------------------------------------|
| • <b>Vladimir Balan</b> ( <i>Bucharest, Romania</i> ) | • <b>Volodymyr Lyubashenko</b> ( <i>Kyiv, Ukraine</i> )  |
| • <b>Taras Banakh</b> ( <i>Lviv, Ukraine</i> )        | • <b>Sergiy Maksymenko</b> ( <i>Kyiv, Ukraine</i> )      |
| • <b>Dmytro Bolotov</b> ( <i>Kharkiv, Ukraine</i> )   | • <b>Koji Matsumoto</b> ( <i>Yamagata, Japan</i> )       |
| • <b>Vyacheslav Boyko</b> ( <i>Kyiv, Ukraine</i> )    | • <b>Piotr Mormul</b> ( <i>Warsaw, Poland</i> )          |
| • <b>Yulia Fedchenko</b> ( <i>Odesa, Ukraine</i> )    | • <b>Maryna Nesterenko</b> ( <i>Kyiv, Ukraine</i> )      |
| • <b>Oleg Gutik</b> ( <i>Lviv, Ukraine</i> )          | • <b>Roman Popovych</b> ( <i>Kyiv, Ukraine</i> )         |
| • <b>Olena Karlova</b> ( <i>Chernivtsi, Ukraine</i> ) | • <b>Alexandr Prishlyak</b> ( <i>Kyiv, Ukraine</i> )     |
| • <b>Volodymyr Kiosak</b> ( <i>Odesa, Ukraine</i> )   | • <b>Aleksandr Savchenko</b> ( <i>Kherson, Ukraine</i> ) |
| • <b>Nadiia Konovenko</b> ( <i>Odesa, Ukraine</i> )   |                                                          |

#### ORGANIZING COMMITTEE

- |                                                     |                                                      |
|-----------------------------------------------------|------------------------------------------------------|
| • <b>Nadiia Konovenko</b> ( <i>Odesa, Ukraine</i> ) | • <b>Bohdan Mazhar</b> ( <i>Kyiv, Ukraine</i> )      |
| • <b>Yuliya Fedchenko</b> ( <i>Odesa, Ukraine</i> ) | • <b>Sergiy Maksymenko</b> ( <i>Kyiv, Ukraine</i> )  |
| • <b>Mykola Lysynskiy</b> ( <i>Kyiv, Ukraine</i> )  | • <b>Alexandr Prishlyak</b> ( <i>Kyiv, Ukraine</i> ) |

## REFERENCES

- [1] Enzo Bonacci. *Studio sperimentale sulla cristallizzazione dell'acido citrico*, volume 40 of *Diritto di Stampa*. Rome: Aracne Editrice, 2013.
- [2] Enzo Bonacci. A Pioneering Experimental Study on the Batch Crystallization of the Citric Acid Monohydrate. *Journal of Chemistry and Chemical Engineering*, 8(6): 611–620, 2014.
- [3] Enzo Bonacci. The Agitation Effects on the Batch Crystallization of the CAM. *International Journal of Mathematical Sciences and Applications*, 7(1): 65–71, 2017.
- [4] Marco Bravi & Barbara Mazzarotta. Primary Nucleation of Citric Acid Monohydrate: Influence of Selected Impurities. *Chemical Engineering Journal*, 70(3): 197–202, 1998.
- [5] Marco Bravi & Barbara Mazzarotta. Size Dependency of Citric Acid Monohydrate Growth Kinetics. *Chemical Engineering Journal*, 70(3): 203–207, 1998.
- [6] Theodorus Nicolaas Zwitering. Suspending of Solid Particles in Liquid by Agitators. *Chemical Engineering Science*, 8(3–4): 244–253, 1958.

## On representation type of incident algebras of extensions of positive posets

**Vitaliy Bondarenko**

(Institute of Mathematics of NAS of Ukraine, Kyiv, Ukraine)

*E-mail:* vitalij.bond@gmail.com

**Maryna Styopochkina**

(Polissia National University, Zhytomyr, Ukraine)

*E-mail:* stmar@ukr.net

In 1972, P. Gabriel introduced a quadratic form for finite quivers, which was called by him the Tits quadratic form. He proved that a quiver  $Q$  is of finite representation type over a field  $k$  (i.e., has up to equivalence finitely many indecomposable representations) if and only if its Tits quadratic form is positive. This result laid the foundations of a new direction in the theory of algebras.

In 1974, Yu. A. Drozd showed that a (finite) poset  $S$  is of finite representation type if and only if its quadratic Tits form

$$q_S(z) = z_0^2 + \sum_{i \in S} z_i^2 + \sum_{i < j, i, j \in S} z_i z_j - z_0 \sum_{i \in S} z_i$$

is weakly positive, i.e., positive on the non-zero vectors with non-negative coordinates (representations of posets were introduced by L. A. Nazarova and A. V. Roiter in 1972). In contrast to quivers, the posets with weakly positive and with positive Tits forms do not coincide. Since the connected quivers having positive Tits quadratic form coincide with the quivers whose underlying graphs are (simply faced) Dynkin diagrams, the posets with positive Tits form are analogs of the Dynkin diagrams. Such posets, which are simply called positive, were classified by the authors in [1]. Up to isomorphism and duality, the positive posets consist of 5 series and 108 discrete ones.

Since the incidence algebras of positive posets are of finite representation type, it is natural to study representation type of their element-extensions. We consider cases when “new elements” are nodes (in the sense that they are comparable with all other elements). Here we formulate some consequences of our investigation.

A positive poset  $T$  is called serial if there exists infinite consequence  $T \subset T_1 \subset T_2 \subset \dots$  such that all posets  $T_i$  are also positive. By definition, the incidence algebra  $\mathcal{I}_k(T)$  of a poset  $T$  of order  $n$  is the matrix algebra which consists of all matrices  $M = (m_{ij})$ ,  $i, j \in T$  (over a field  $k$ ) such

that  $m_{ij} = 0$  if  $i > j$ . Finally, we write  $X > Y$  for subposets  $X, Y$  of a poset  $T$  if  $x > y$  for any  $x \in X, y \in Y$ .

**Theorem 1.** *Let  $S$  be a positive poset and  $\bar{S} = S \cup X$  be an extension of  $S$  with chained  $X > S$ . Then the incidence algebra  $\mathcal{I}_k(\bar{S})$  is of infinite representation type if the length  $l(X)$  of  $X$  is greater than 5.*

**Theorem 2.** *Let  $\bar{S}$  be as in Theorem 1 but  $S$  is non-serial. Then the incidence algebra  $\mathcal{I}_k(\bar{S})$  is of infinite representation type if*

- (a) *the width of  $S$  is equal to 2 and  $l(X) > 4$ ;*
- (b) *the width of  $S$  is equal to 3 and  $l(X) > 1$ .*

In all statements the estimates are exact.

#### REFERENCES

- [1] V. M. Bondarenko, M. V. Styopochkina. (Min, max)-equivalence of partially ordered sets and the Tits quadratic form. *Collection of works of Inst. of Math. NAS Ukraine – Problems of Analysis and Algebra*, 2(3) : 18–58, 2005.

## A theorem on hypercohomology groups and singular homology in field theory

Francisco Bulnes

(IINAMEI, Research Department in Mathematics and Engineering, TESCHA)

*E-mail:* francisco.bulnes@tesch.edu.mx

In this research we consider a theorem that relates the hypercohomology groups obtained with the spectrum through the its singular homology taking components  $\mathbb{Z}_{tr}(k)$  and the  $A_1$  -homotopy in the action of the symmetric  $DM_{Nis}^{eff,-}(k)$ . Then we can characterize in a projective vector bundle the solutions of the field equations  $dda = 0$  on singularities.

#### REFERENCES

- [1] Bulnes, F., *Tensor Triangulated Category to Quantum Version of Motivic Cohomology on Étale Sheaves*, LJRS Volume 23 Issue 16.
- [2] Prof. Dr. Francisco Bulnes, *Geometrical Motives Commutative Diagram to the derived category DQFT*, Int. J. Adv. Appl. Math. and Mech. 10(4) (2023) 17– 22.
- [3] Bulnes F. Extended d-cohomology and integral transforms in derived geometry to QFT-equations solutions using Langlands correspondences. *Theoretical Mathematics and Applications*. 2017;7(2):51-62

## Geometric and algebraic-topological structures in Schwartz distribution spaces for relativistic Quantum Mechanics

David Carfi

(Department of Physics, University of Messina, Italy)

*E-mail:* dcarfi@unime.it

The classic Hilbert space methods cannot be used for the definition and resolution of the free relativistic Schrödinger equation because the very fundamental solutions of this equation cannot be framed in a Hilbert or Banach space context. We can justify the necessity to use distribution theory, for many reasons. If we lock down ourselves in separable Hilbert space theory, we cannot

## Table of contents

|                                                                                                                                                       |           |
|-------------------------------------------------------------------------------------------------------------------------------------------------------|-----------|
| <b>A. Sako</b> <i>Solutions of <math>N</math>-body harmonic oscillators and Calogero-Moser model using <math>\Phi^4</math> matrix model</i>           | <b>2</b>  |
| <b>B. El Alaoui</b> <i>Partitioning problem and defensive alliances in the context of zero-divisor graphs of rings</i>                                | <b>3</b>  |
| <b>M. Amram</b> <i>On the connection between algebraic, geometric, and topological methods in the classification of algebraic surfaces and curves</i> | <b>4</b>  |
| <b>N. Ando</b> <i>Nilpotent structures of oriented neutral vector bundles</i>                                                                         | <b>6</b>  |
| <b>M.J. Atteya</b> <i>Multiplicative <math>b</math>-homogeneralized Derivations of Associative Rings</i>                                              | <b>8</b>  |
| <b>T. Banakh</b> <i>Algebra in fields extended by infinity</i>                                                                                        | <b>9</b>  |
| <b>M. Bisci</b> <i>Variational problems in Nonsmooth Analysis</i>                                                                                     | <b>10</b> |
| <b>D. Bolotov</b> <i>On 2-convex embeddings of non-orientable surfaces in four-dimensional Euclidean space</i>                                        | <b>11</b> |
| <b>E. Bonacci</b> <i>Mixing optimization in the batch crystallization of CAM</i>                                                                      | <b>11</b> |
| <b>V. Bondarenko, M. Styopochkina</b> <i>On representation type of incident algebras of extensions of positive posets</i>                             | <b>12</b> |
| <b>F. Bulnes</b> <i>A theorem on hypercohomology groups and singular homology in field theory</i>                                                     | <b>13</b> |
| <b>D. Carfi</b> <i>Geometric and algebraic-topological structures in Schwartz distribution spaces for relativistic Quantum Mechanics</i>              | <b>13</b> |
| <b>Y. Chapovskyi, S. Koval, O. Zhur</b> <i>Lie subalgebras of real order-three special linear Lie algebra revisited</i>                               | <b>16</b> |
| <b>Y. Cherevko, O. Chepurna, Y. Kuleshova</b> <i>Conformal mappings and a non-holonomic frame</i>                                                     | <b>18</b> |
| <b>A. Chornenka, O. Gutik</b> <i>On topologization of the bicyclic monoid</i>                                                                         | <b>19</b> |
| <b>J. Cuadros, J. Lope</b> <i>An Application to Sasaki Extremal metrics via the Berglund-Hübsch rule</i>                                              | <b>20</b> |
| <b>E. Sevost'yanov, V. Desyatka</b> <i>On singularities of mappings with a Lebesgue integrable majorant</i>                                           | <b>22</b> |
| <b>I. Diamantis, S. Lambropoulou, S. Mahmoudi</b> <i>New Combinatorial Invariants of Doubly Periodic Tangles</i>                                      | <b>24</b> |
| <b>K. v. Dichter</b> <i>Inequalities involving means in high-dimensional spaces</i>                                                                   | <b>25</b> |
| <b>P. Petrenko, A. Andreev</b> <i>Two problems in the theory of metric preserving functions</i>                                                       | <b>27</b> |
| <b>Y. Drozd</b> <i>Group action on noncommutative curves</i>                                                                                          | <b>29</b> |